

# Modelling and Analysis of Power Consumption for Component-based Embedded Software <sup>\*</sup>

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**Abstract.** With the increasing complexity of the real-time embedded software, the power consumption is becoming a real challenge in the system designs. In this paper, for modelling the component-based embedded software, the interface automata is extended by adding time intervals on the actions and assigning energy consumption rates on the states. The extensional formalism is called *energy interface automata*. Then the system designs are modelled by energy interface automaton networks which consist of a set of energy interface automata synchronized by shared actions. Based on analyzing the integer state space of the energy interface automaton networks and its compatible reachability graph, we develop two algorithms for the problem of the minimal energy consumption calculation and the maximal energy consumption verification respectively.

**Keywords:** embedded software design, power-aware computing, component-based design, real-time system, model checking, interface automata.

## 1 Introduction

In recent years, as the result of the increasing complexity of real-time embedded systems which also have high performance demands, the embedded software raises many challenges to current software techniques. Especially for the power consumption issues, new methodologies and tools are required to deal with it at all abstraction levels. Currently, many approaches have been proposed to reduce total power consumption, such as: the dynamic voltage scaling (DVS), dynamic power management (DPM), as well as many other studies on the energy-aware schedule schemes, and so on. However, most approaches to energy analysis of the embedded software require the system to be completely developed, depending

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on either measurement on a hardware prototype or detailed simulation of the entire system. From the viewpoint of software engineering, typically the traditional process is too late in the design cycle to perform high-level or architectural optimizations. And it is important to model, analyze and check the power consumption characteristics at the abstraction level of the system design, without consideration of too much details of the hardware or platform.

In this paper, considering the component-based embedded software designs we extend the interface automata[1] by adding time intervals on the actions and assigning energy consumption rates on the states to describe the energy-aware behaviors of software components. The extensional formalism is called *energy interface automata (EIA)*. And the system designs are modelled by energy interface automaton networks which consist of a set of energy interface automata synchronized by shared actions. The rest of paper is organized as follows. Section 2 gives the description of the problems we concern and the basic idea of power consumption rates. In section 3, we introduce the interface automata model and the energy interface automata networks, and give the formal definitions for analysis and verification. In section 4 and 5, based on constructing and investigating the compatible reachability graph of the integer state space of the system design models, we develop algorithms to solve the problems of minimal energy consumption calculation and maximal energy consumption verification respectively. The last section includes the related work and the conclusion.

## 2 Problem Statement

In this work, we mainly consider the following power consumption problems:

**Minimal Energy Consumption Calculation** : Given a special state of a component-based embedded software system, how much energy should be consumed at the least, while the system can operate without any mistake from the initial state to that special one?

**Maximal Energy Consumption Verification** : Given the time constraint, power limitation and the special state of the system, does the total amount of the energy consumption satisfy the given power limitation when the system reaches the special state within the time constraint?

Based on the observation that there are different kinds of power-aware characteristics of hardware in embedded systems (for example, most power supply devices have the busy, idle and sleep modes changing along with the system states to reduce the power consumption), we can make a reasonable assumption that *there are different power consumption rates on different states of the embedded software system, and furthermore, those rates could be any nonnegative real number, not just be several simple modes.*

### 3 Modelling the System Behaviors

#### 3.1 Interface Automata(IA) Model

Interface automaton[1] is a light-weight formal language to describe the order of the interactions between the software component and its environment. The basic idea is that when the components are composed, their environment assumptions should be also composed. Accordingly, if there are *some* helpful environments satisfy both of their environment assumptions, these components are considered compatible. The formal definitions are given below.

**Definition 1.** An *interface automaton (IA)* is a tuple  $P = (V_P, v_P^{Init}, A_P^I, A_P^O, A_P^H, \Gamma_P)$  where:

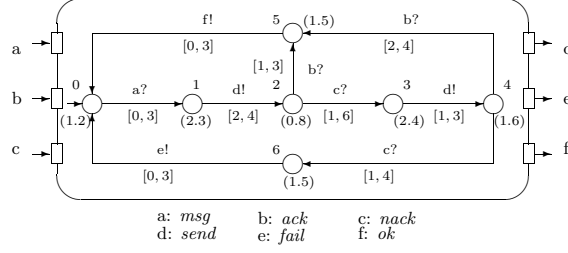
- $V_P$  is a finite set of states, each state  $v \in V_P$ ;
- $v_P^{Init} \in V_P$  is the initial state;
- $A_P^I, A_P^O$  and  $A_P^H$  are mutually disjoint sets of input, output and internal actions, and  $A_P = A_P^I \cup A_P^O \cup A_P^H$  is the set of all actions;
- $\Gamma_P \subseteq V_P \times A_P \times V_P$  is a set of transitions. □

#### 3.2 Energy Interface Automata(EIA) and the EIA-Networks

Essentially the amount of energy consumption has a close relationship with the running time of the system. So we need to extend the interface automata with both of time and energy semantics to describe the system power-aware behaviors. Fig.1 shows an example of an energy interface automata model of component *communication*, which is an extensional energy version of the *IA* model proposed in [1]. On each action there is a time interval indicates the demand of time constraint, and on each state there is a nonnegative real number represents how much energy is consumed in 1 time units, the *power consumption rate*. For example, in state 1, the notation of time interval [2,4] indicates that the system should stay here at least 2 time units, at most 4 time units, and the real number 1.2 in state 0 denotes that the energy consumption is 1.2 in 1 time unit when system stay in there.

**Definition 2.** An *energy interface automaton(EIA)* is a tuple  $P = (V_P, F_P, A_P, I_P, \Gamma_P)$  where:

- $V_P$  is a finite set of states, each state  $v \in V_P$ ; and there is an initial state  $v_P^{init}$  at most;
- $F_P : V_P \mapsto R^+$  is a function which maps each state to a nonnegative real number;
- $A_P$  is the set of all actions, each action  $a \in A_P$ , and it include the  $A_P^I, A_P^O$  and  $A_P^H$ , the mutually disjoint set of input, output and internal actions respectively;
- $I_P$  is a finite set of time intervals; each interval has the form of  $[x, y]$  where  $x, y$  are nonnegative integer numbers ( $x \leq y, y \neq \infty$ );
- $\Gamma_P \subseteq V_P \times A_P \times I_P \times V_P$  is a set of transitions.



**Fig. 1.** The EIA model of component *communication*

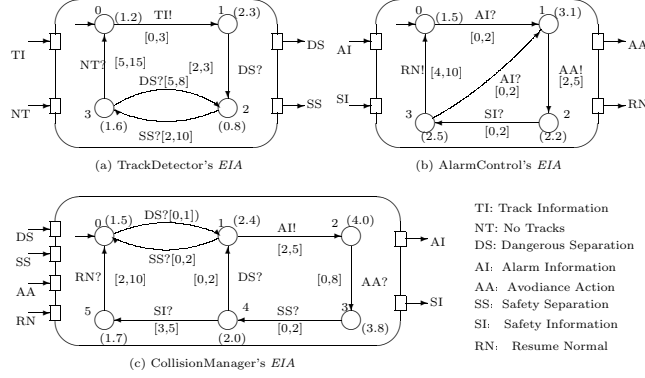
□

We use a *timed energy state sequence* with a form of  $\sigma = v_0 \xrightarrow{a_0, \tau_0} v_1 \xrightarrow{a_1, \tau_1} \dots \xrightarrow{a_{m-1}, \tau_{m-1}} v_m \xrightarrow{a_m, \tau_m} v_{m+1}$  to represent a power consumption behavior starting from the initial state. Accordingly there is a power rates sequence:  $e_0 \hat{e}_1 \hat{e}_2 \dots \hat{e}_m \hat{e}_{m+1}$  such that each  $e_i = F_P(v_i)$  ( $0 \leq i \leq m+1$ ). The semantics of the behavior  $\sigma$  is that the system starts at state  $v_0$ , after  $\tau_0$  time units it changes to  $v_1$  through the transition ignited by the action  $a_0$  and staying there for  $\tau_1$  time units, and the power consumption in state  $v_0$  and  $v_1$  are  $e_0 \times \tau_0$  and  $e_1 \times \tau_1$  respectively, and so on.

For modelling the component-based embedded software, we use the *energy interface automaton networks (EIA-Networks)* to represent the power-aware behaviors of the compositional system. Since an input action of one interface automaton may coincide with an output action of the other, these two interface automata will synchronize on such shared actions, asynchronously interleaving on other actions. Those synchronized actions between any two interface automata  $(P_i, P_j)$  are denoted by  $shared(P_i, P_j) = A_{P_i} \cap A_{P_j} = (A_{P_i}^O \cap A_{P_j}^I) \cup (A_{P_i}^I \cap A_{P_j}^O)$ . More details about interface automata composition can be found in [1]. Fig.2 shows a simple version of TCAS (Traffic Collision Avoidance System) designs.

**Definition 3.** Let  $N = (K, Z, F_N)$  be an *EIA-Networks* where  $K = \{P_1, P_2, \dots, P_n\}$ , each  $P_i = (V_{P_i}, F_{P_i}, A_{P_i}, I_{P_i}, \Gamma_{P_i})$  ( $1 \leq i \leq n$ ), and  $Z = \{a \in shared(P_i, P_j) \mid 1 \leq i, j \leq n, i \neq j\}$  is a set of all shared actions,  $n$  denotes the total number of components in system. The states and actions are defined as below:

- an *untimed energy state*  $\bar{v}$  of  $N$  is in  $V_{P_1} \times V_{P_2} \times \dots \times V_{P_n}$ , that is,  $\bar{v} = (v_1, v_2, \dots, v_n)$  ( $v_i \in V_{P_i}, 1 \leq i \leq n$ ). The *initial untimed energy state* of  $N$  is  $\bar{v}_N^{init} = (v_{P_1}^{init}, v_{P_2}^{init}, \dots, v_{P_n}^{init})$ ;
- an *energy state*  $u$  of  $N$  is a pair  $u = (\bar{v}, c)$  where  $\bar{v} = (v_1, v_2, \dots, v_n)$  is an untimed state of  $N$  and  $c : \{v_i \mid 1 \leq i \leq n\} \mapsto R^+ \cup \{0\}$  is called the *clock function* which maps each  $v_i$  to a nonnegative real number that indicates for the  $P_i$  how long the system has been staying at  $v_i$ . The *initial energy state* of  $N$  is  $u_N^{init} = (\bar{v}_N^{init}, c^{init})$  where  $\bar{v}_N^{init}$  is the initial untimed energy state of



**Fig. 2.** An EIA-Networks of the TCAS system

- $N$  and  $c^{init}(v_{P_i}^{init}) = 0$  for any  $i(1 \leq i \leq n)$ . The set of energy states of  $N$  is denoted by  $U_N$ ;
- $F_N : U_N \mapsto \{E_0, E_1, \dots, E_{|U_N|}\}$  is a power consumption function which maps each state  $u$  to a vector  $E = \langle e_1, e_2, \dots, e_n \rangle$ , where each  $e_i = F_{P_i}(v_i)(1 \leq i \leq n)$ ;
  - the set of actions of  $N$  is  $A_N = A_N^I \cup A_N^O \cup A_N^H$ , where the set of input actions is  $A_N^I = \left( \bigcup_{1 \leq i \leq n} A_{P_i}^I \right) / Z$ , the set of output actions is  $A_N^O = \left( \bigcup_{1 \leq i \leq n} A_{P_i}^O \right) / Z$ , and the set of internal actions is  $A_N^H = \left( \bigcup_{1 \leq i \leq n} A_{P_i}^H \right) \cup Z$ .
  - the set of time intervals of  $N$  is  $I_N = \bigcup_{1 \leq i \leq n} I_{P_i}$ .  $\square$

The transitions of  $N$  is defined as follows:

**Definition 4.** Let  $N = (K, Z, F_N)$  be an *EIA-Networks* where  $K = \{P_1, P_2, \dots, P_n\}$ , each  $P_i = (V_{P_i}, F_{P_i}, A_{P_i}, I_{P_i}, \Gamma_{P_i})(1 \leq i \leq n)$ , and  $u = (\bar{v}, c)$  and  $u' = (\bar{v}', c')$  be its states where  $\bar{v} = (v_1, v_2, \dots, v_n)$  and  $\bar{v}' = (v'_1, v'_2, \dots, v'_n)$ , the corresponding power consumption vectors are  $E = \langle e_1, e_2, \dots, e_n \rangle$ ,  $E' = \langle e'_1, e'_2, \dots, e'_n \rangle$ . Then the system can change from the state  $u$  to  $u'$  by a transition within a delay  $d$  (denoted by  $u \xrightarrow{a,d} u'$ ), if one of the following conditions holds:

- for an action  $a \notin Z$ , there is a transition  $(v_k, a, [x_k, y_k], v'_k) \in \Gamma_{P_k}$  ( $1 \leq k \leq n$ ) satisfying  $x_k \leq c(v_k) + d \leq y_k$  and  $c'(v'_k) = 0$ ,  $e'_k = F_{P_k}(v'_k)$ . At the same time  $v_i = v'_i$ ,  $c'(v_i) = c(v_i) + d$  and  $e'_i = e_i$  for any  $i$  ( $i \neq k, 1 \leq i \leq n$ ); or
- for an action  $a \in \text{shared}(P_i, P_j)(1 \leq i, j \leq n, i \neq j)$ , there are transitions  $(v_i, a!, [x_i, y_i], v'_i) \in \Gamma_{P_i}$  ( $a!$  denote  $a$  is an output action) and  $(v_j, a?, [x_j, y_j], v'_j) \in \Gamma_{P_j}$  ( $a?$  denote  $a$  is an input action) satisfying  $x_i \leq c(v_i) + d \leq y_i$ ,  $x_j \leq c(v_j) + d \leq y_j$ ,  $c'(v'_i) = 0$ ,  $c'(v'_j) = 0$  and  $e'_i = F_{P_i}(v'_i)$ ,  $e'_j = F_{P_j}(v'_j)$ . At the same time,  $v_k = v'_k$ ,  $c'(v_k) = c(v_k) + d$  and  $e'_k = e_k$  for any  $k(k \neq i, j, 1 \leq k \leq n)$ .  $\square$

Then a behavior of  $N$  can be denoted as a timed energy state sequence:  $\sigma = u_0 \xrightarrow{a_0, d_0} u_1 \xrightarrow{a_1, d_1} \dots \xrightarrow{a_{m-1}, d_{m-1}} u_m \xrightarrow{a_m, d_m} u_{m+1}$  where  $u_0$  is the initial state of  $N$ . And for each behavior there is a corresponding vector sequence  $E_0 \hat{E}_1 \hat{E}_2 \dots \hat{E}_{m+1}$ , where each  $E_i = \langle e_{i1}, e_{i2}, \dots, e_{in} \rangle$  has the same size of  $n$ . We use the  $delay(\sigma)$  to denote the total time delay of a behavior, that is,  $delay(\sigma) = \sum_{i=0}^m d_i$ , and the  $cost(\sigma)$  to represent the total power consumption of the behavior, that is,  $cost(\sigma) = \sum_{i=0}^m (d_i \times \sum_{j=1}^n e_{ij})$ .

## 4 Constructing the Integer Reachability Graph

Since the delay  $d$  could be any nonnegative real number, it is clear that the state space of *EIA-Networks*  $N$  is infinite. We need to deal with the power consumption problems in a finite way. Let  $\sigma = u_0 \xrightarrow{a_0, d_0} u_1 \xrightarrow{a_1, d_1} \dots \xrightarrow{a_{m-1}, d_{m-1}} u_m \xrightarrow{a_m, d_m} u_{m+1}$  be a behavior of  $N$ . If  $d_i$  is an integer for any  $i$  ( $0 \leq i \leq m$ ), then the  $\sigma$  is called an *integer behavior*. It follows that any state  $((v_1, v_2, \dots, v_m), c)$  occurring in an integer behavior satisfies  $c(v_j)$  is an integer for any  $j$  ( $1 \leq j \leq m$ ), which is called an *integer state*.

**Lemma 1.** For each behavior  $\sigma$  of an *EIA-Networks*  $N$ , there are integer behaviors  $\sigma'$  and  $\sigma''$  satisfying  $cost(\sigma'') \geq cost(\sigma) \geq cost(\sigma')$ .  $\square$

**Theorem 1.** Let  $N$  be an *EIA-Networks*,  $u$  be any state of  $N$ ,  $C$  be a set of behavior in which each element has the form of  $u_0 \hat{E}_1 \hat{E}_2 \dots \hat{E}_m u$ , and  $R$  be a real number, then for each  $\sigma \in C$  satisfying  $cost(\sigma) \geq R$  if and only if there is an integer behavior  $\sigma' \in C$  satisfying  $cost(\sigma') \geq R$ .  $\square$

In the case of  $cost(\sigma) \leq R$ , there is a similar result. Therefore, for the problem in this paper we only need to consider the integer state space of an *EIA-Networks*.

Based on theorem 1, we can construct a reachability graph  $G = \{S, L\}$  for an *EIA-Networks*  $N$  as follows, where  $S$  is a set of nodes and  $L$  is a set of edges:

1. for the initial state  $u_N^{Init}$  of  $N$ ,  $u_N^{Init}$  is in the set  $S$ , which is called *initial node* denoted by  $s_0$ ;
2. for the other state  $u$ , if there is a transition  $u \xrightarrow{a, d} u'$ , then  $u'$  is in the set  $S$ , and there is an corresponding edge with a form of  $s \xrightarrow{l} s'$ , where  $l$  is the label on the edge,  $l = (a, d)$ .

Notice that one automaton may produce an output event that is an input event of another automaton, but it is not accepted by the latter one. It means that there are some contradictions between the environment assumptions of these two automata which have shared actions. When this happens, those corresponding states of  $N$  are called *illegal states*. An maximum fixpoint algorithm has been presented to compute the compatible composition of interface automata by removing the set of *illegal(N)* recursively[1]. As a result we can denote by  $com(N)$  the *compatible EIA-Networks* which only includes the compatible states of  $N$ .

Then we can also get a compatible reachability graph  $com(G)$  which only consists of those nodes corresponding to the set of compatible states. If  $com(G)$  is nonempty, it indicates that there is a helpful environment to make the  $N$  running normally. Based on the construction of reachability graph, we can further conclude that each compatible integer behavior of *EIA-Networks* is corresponding to a path in the  $com(G)$ , and vice versa.

## 5 Analysis and Verification of System Power Consumption

Let  $\rho$  be a path of the compatible reachability graph  $com(G)$  with a form of  $\rho = s_0 \xrightarrow{l_0} s_1 \xrightarrow{l_1} \dots \xrightarrow{l_{m-1}} s_m$  in which  $l_i = (a_i, d_i)$  ( $0 \leq i < m$ ). Based on the discussion in the above section, several concepts are introduced as follows:

- **consumption rate vector:** For each node  $s_i$  of  $com(G)$ , there is a corresponding vector  $E_i = \langle e_{i1}, e_{i2}, \dots, e_{in} \rangle$ , and each  $e_{ij}$  ( $1 \leq j \leq n$ ) indicates the power consumption rate of component  $j$  in the compositional state  $u_i$  which is corresponding to the node  $s_i$ ;
- **consumption matrix:** For each path  $\rho$  in  $com(G)$ , we can construct a matrix such that  $E_\rho = (E_0, E_1, \dots, E_{m-1})_{m \times n}^T$  ( $m$  denotes the length of the path);
- **time delay vector:** For each path  $\rho$  in  $com(G)$ , there is a time delay vector with a form of  $D_\rho = \langle d_0, d_1, \dots, d_{m-1} \rangle$ , and the total time delay of the path is  $T_\rho = \sum_{i=0}^{m-1} d_i$ ;
- **consumption of the path:** For each path  $\rho$  in  $com(G)$ , the power consumption is  $\varepsilon_\rho = \sum_{i=1}^n (D_\rho \times E_\rho)_{0i}$ , where  $D_\rho \times E_\rho$  can be denoted as

$$(d_0, d_1, \dots, d_m) \times \begin{pmatrix} e_{01} & e_{02} & \dots & e_{0n} \\ e_{11} & e_{12} & \dots & e_{1n} \\ \vdots & \vdots & \ddots & \vdots \\ e_{(m-1)1} & e_{(m-1)2} & \dots & e_{(m-1)n} \end{pmatrix}$$

In fact, the size of  $D_\rho \times E_\rho$  is  $1 \times n$  with a form of  $C_\rho = (c_1, c_2, \dots, c_n)$ , and each  $c_i$  is exactly corresponding to the  $i$ th component's power consumption along with the path  $\rho$ .

### 5.1 The minimal consumption calculation problem

Notice that usually the given system states we concern are the untimed states, but in the *EIA-Networks* each special system state has been divided into several integer timed energy states which have the same untimed state with different time stamps. That is, for a special system state  $u_j$ , accordingly there are a set of different timed nodes in  $com(G)$ . We use  $\delta(u_j)$  to denote it.

Now given a set of finite node  $\delta(u_j)$  in  $com(G)$ , let  $\rho(s_j)$  be the set of path in which each element is a reachable path starting from the initial node  $s_0$  to a timed node  $s_j$ . Then the problem can be described again as follows:

Given a set of finite node  $\delta(u_j)$  in  $com(G)$ , which one in the set of path  $\rho(\delta(u_j))$  satisfies  $\varepsilon = \min\{\varepsilon_{\rho'} | \rho' \in \rho(\delta(u_j))\}$ ?

We call that path the *minimal consumption path*.

**Theorem 2.** For each node of the compatible reachability graph  $com(G)$ , its minimal consumption path is a simple path.  $\square$

A simple path in  $com(G)$  is a path without any loops. Based on the above theorem, we can develop an algorithm to find out which one is the minimal consumption path. The algorithm is depicted in Fig.3. The variable *min\_omega* is used to store the value of minimum energy consumption, and the *min\_omega\_path* is a set variable used to store the minimal consumption paths. The path in  $com(G)$  that we have so far searched is stored in the variable *current\_path*. For the given state  $u_j$ , the algorithm traverse the reachability graph  $com(G)$  by a depth first search manner to check all the simple paths between the initial state  $s_0$  and one certain state in  $\delta(u_j)$ , through calculating and comparing the energy consumption of each path. At the same time, the detail information about the minimal consumption path will be recorded in the set of *mini\_omega\_path*. Since there is only a finite number of simple paths in  $com(G)$  and the algorithm is based on depth first search framework, the complexity of the algorithm is proportional to number and length of simple paths in  $com(G)$ .

```

min_omega:=∞ ;ε:=0; min_omega_path:=∅; current_path:=⟨ s0 ⟩;
repeat node:= the last node of current_path;
if node has no new successive node then delete the last node of current_path;
else begin node:= a new successive node of node;
if node∈δ(uj)
then begin
if the power consumption of the path current_path
satisfies ε < min_omega
then begin
min_omega:=ε;
min_omega_path:=⟨ ⟩;
min_omega_path:=current_path∪ ⟨ sj ⟩;
end
end
else append node to current_path;
end
until current_path=⟨ ⟩

```

**Fig. 3.** Algorithm for the minimum power consumption calculation

Once we get the minimal consumption path, it's easily to obtain some other power properties of system. Suppose that there is a minimal power consumption path  $\rho_{min}$  with a form of  $\rho_{min} = s_0 \xrightarrow{l_0} s_1 \xrightarrow{l_1} \dots \xrightarrow{l_{m-1}} s_m$ , then



- *minimal power consumption rate of system*:  $H_{min} = \varepsilon_{\rho_{min}}/T_{\rho_{min}}$  which can be provided as a reference for the design of system power supply.
- *peak consumption point of path*: For the path  $\rho_{min}$  if there is a  $s_u$  satisfies  $\Lambda_u = \max\{d_v \cdot \sum_{i=1}^n e_{vi} | 0 \leq v < m\}$  then we call it the *peak consumption point* of that path.
- *minimal power consumption rate of components*: From each  $c_i$  of  $C_{\rho_{min}} = D_{\rho_{min}} \times E_{\rho_{min}}$ , the power consumption of each components can be easily obtained. The  $i$ th component's minimum power rate is  $c_i/T_{\rho_{min}}$ .

## 5.2 The maximum verification problem

In order to solve the maximal energy verification problem, it is necessary to check all paths from the initial node to the given node, comparing the energy consumption of each path to the given power limitation. However, due to the loops in  $com(G)$ , the number of path could be infinite and the length of path could also be infinite. As a result, some expected special states may be unreachable in a finite time and the power consumption is infinite. So we need to consider the semantics of the loops and give some constraints to them: *For each given state, there is a deadline  $T_D$  which shows that within the limitation the system should have changed from initial state to that given state, implementing the expected functionality.* Then for a given node of  $com(G)$  we only consider the finite set of reachable path satisfying the corresponding  $T_D$ .

Based on the assumption and the theorem 1, we can develop a verification algorithm which is depicted in Fig.4. The algorithm traverses the  $com(G)$  in a depth first manner starting from the initial node. We use  $E_D$  to denote the pre-defined amount of energy consumption limitation. The *error\_path* to store the illegal paths, which satisfy the deadline but violating the energy consumption limitation. The boolean variable *satisfied* indicates whether all system behaviors satisfying deadlines without violating the given power consumption. For each new node discovered, the algorithm first check if it is such that the total time delay of the path corresponding to *current\_path* less than the  $T_D$ . If not, then the algorithm backtracks. If yes, then the algorithm further check whether the new node is the given node  $s_j$ . If yes again, then the algorithm continue to compare the energy consumption of the *current\_path* with the  $E_D$ . If the result of the comparison is false, then we put the path into *error\_path* and assign the *satisfied* with *false*. If the new node is not  $s_j$ , then the algorithm adds it into the *current\_path* to begin a new search. Theorem 1 and the above assumption give the guarantee that the algorithm can terminate, and the complexity is proportional to nodes in  $com(G)$ .

## 6 Conclusion

The related work include[2–6]. A prototype is being developed to implement the algorithms proposed in this paper, and will be integrated into the tool set of MCESD (Model checker for Component-based Embedded Software Designs)

```

satisfied := true; error_path:= $\emptyset$ ; current_path:= $\langle s_0 \rangle$  ;
repeat node:= the last node of current_path;
  if node has no new successive node then delete the last node of current_path;
  else begin node:= a new successive node of node;
    if the total time delay of current_path $\hat{\wedge}$ node satisfies  $T_p \leq T_D$ 
    then begin
      if node =  $s_j$ 
      then begin
        if the power consumption of current_path satisfies  $\varepsilon > E_D$ 
        then put current_path $\hat{\wedge}$ node into the set of error_path;
          satisfied := false;
        end
      else append the node to current_path;
      end
    end
  until current_path= $\langle \ \ \rangle$ 
return satisfied.

```

Fig. 4. Algorithm for the maximum power consumption verification

which is based on our preceding works [7, 8]. For future work, we will consider the other kinds of resource properties in component-based embedded software designs, and do more case studies in practical use.

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